

# ***How Many Students Need to be Replaced to Invalidate a Teacher's Evaluation Based on Value-added?***

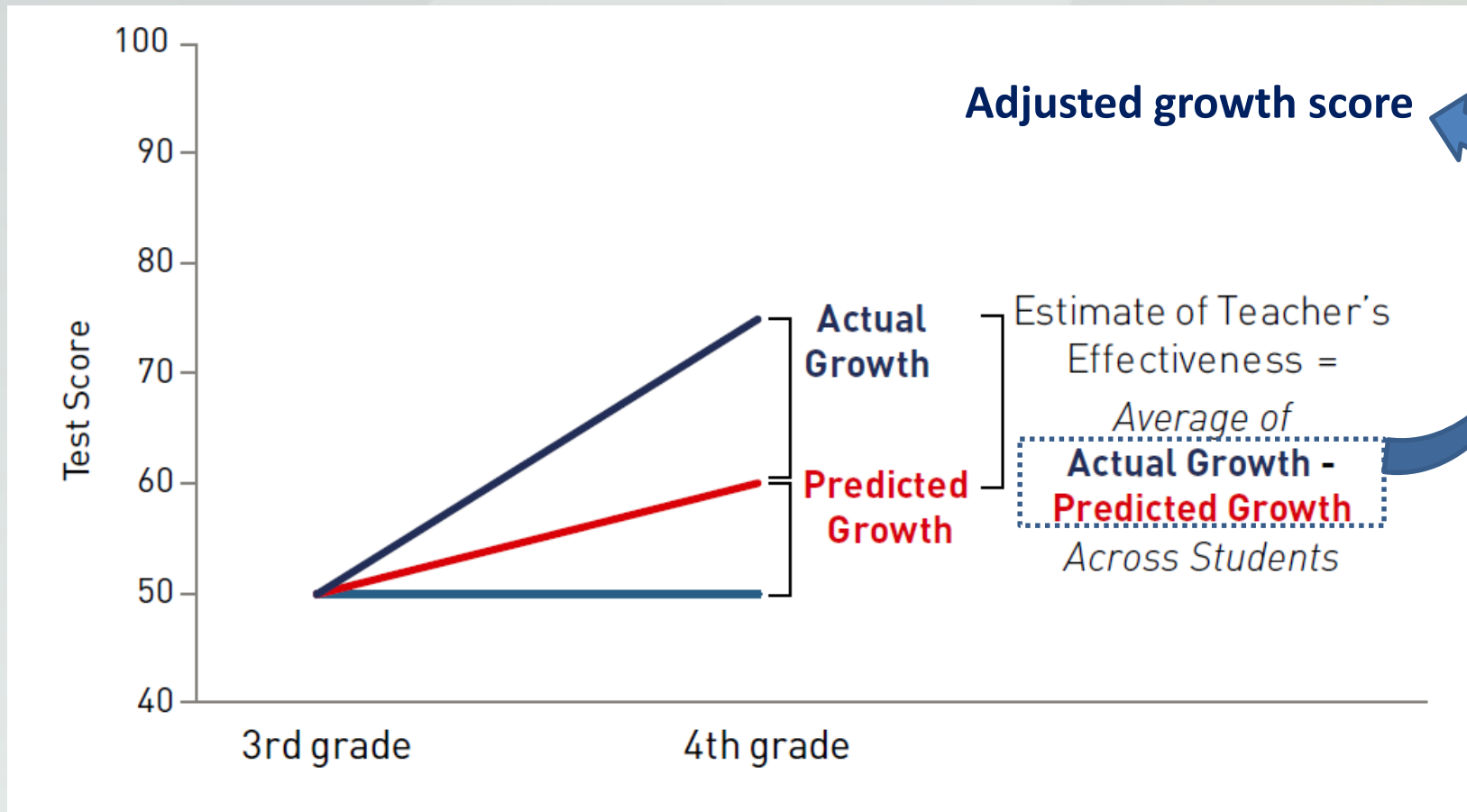
**An Approach to Characterize the Uncertainty,  
Interpret and Make Use of Value-added**

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# Background

- No Child Left Behind and Race to the Top competition
- Some states have already incorporated value-added to inform high-stake decision-making for individual teachers
- **It is essential to know the uncertainty of the measure for such high stakes decisions!** Firing or promoting a teacher based on only an uncertain point estimate may be unfair or create a loss of investment or resources for a school.

# What is value-added?



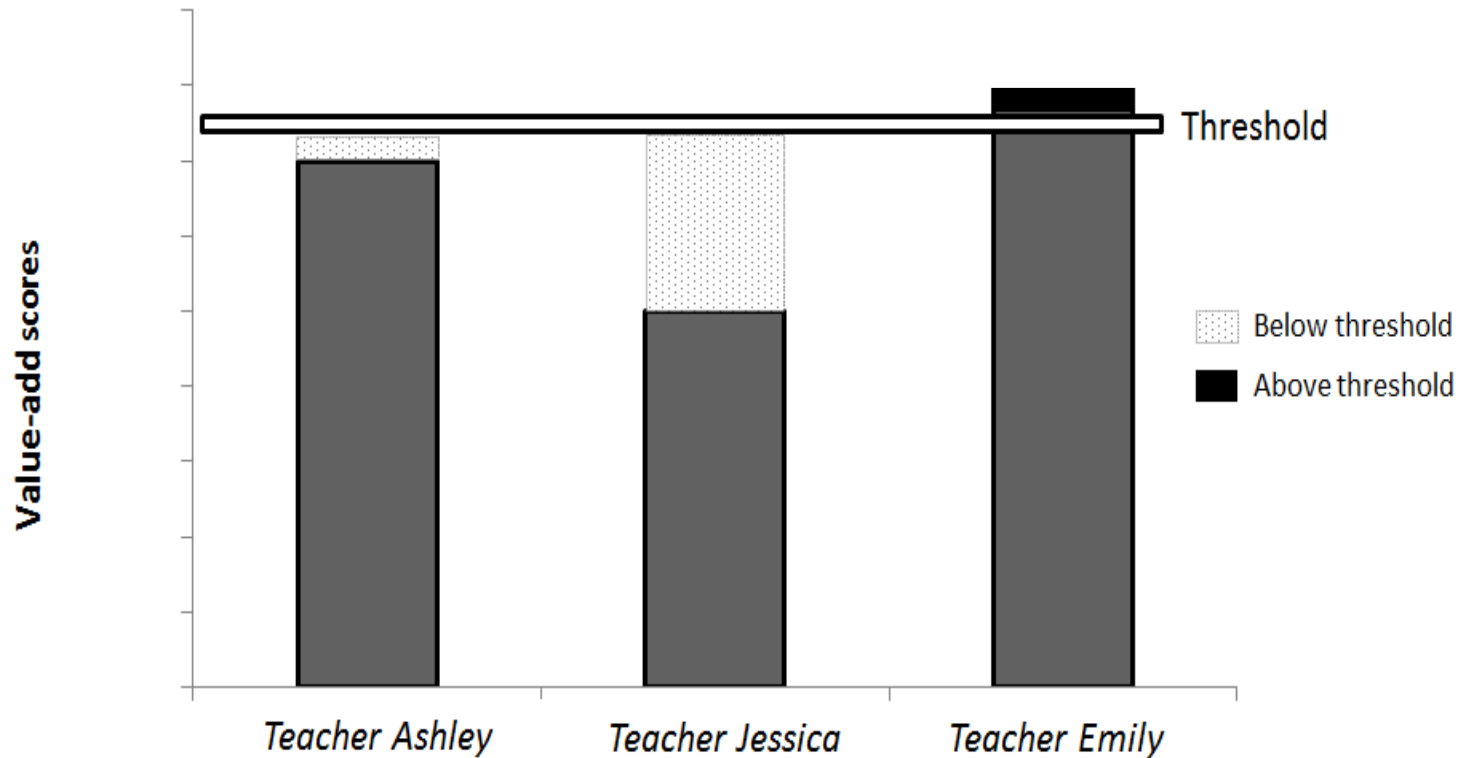
# Uncertainty of value-added

- Concerns about the validity and reliability of value added as a basis to inform high stake decisions:
  - Sorting based on pretests and non-random assignment of teachers to classrooms
  - Availability of test scores
    - It is recommended to have two years of prior tests in the model.
    - It is not uncommon for students (and even teachers) to change school.
  - Unreliability in test scores
    - Measurement errors
    - Different achievement measures

*All these can cause inconsistency of value-added.*

*We summarized these sources of bias as they can lead to violation of the conditional random assignment assumption and thus bring uncertainty to the estimated teacher effect.*

**Figure 2. Teacher Effects Estimated by Value-added  
(Hypothetical)**



- *Dismiss both Ashley and Jessica?*
- *Send whom to professional development?*

# Current approach to quantify the uncertainty

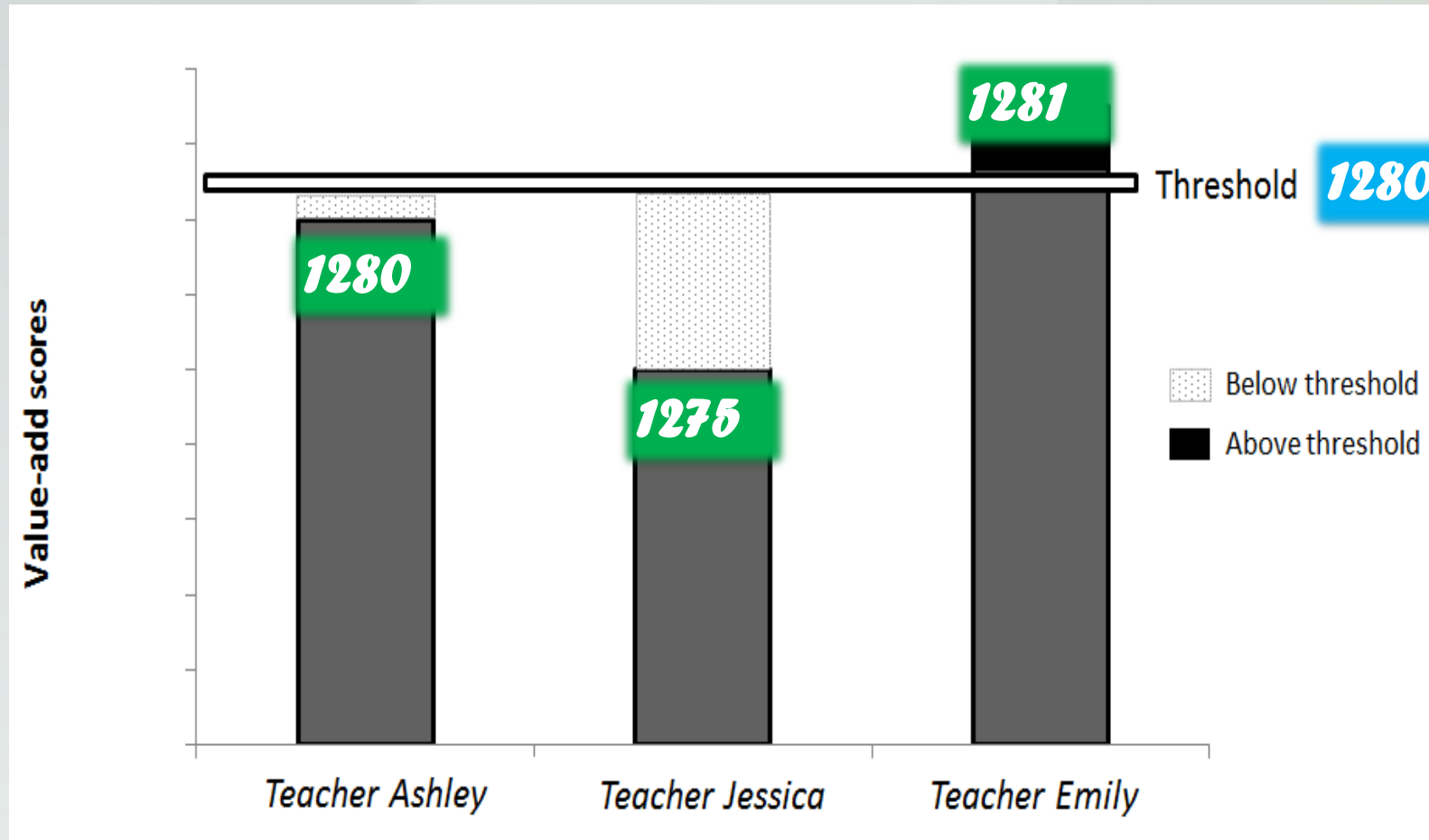
- standard errors or confidence interval
  - based on repeated sampling framework
  - difficult to understand and interpret for a decision regarding a single teacher
  - mainly concern about sampling error but not bias/inconsistency

The goal of this study is to provide an *intuitive* approach to quantify the uncertainty of value-added to inform decision-makings in practical education terms.

# Theoretical Framework

- Replacement idea to quantify the robustness of an inference (Frank, Maroulis, Duong & Kelcey, 2013)
  - what percentage of the samples should be replaced with counterfactual no effect cases to invalidate the inference
- In this study, we ask: *how many students need to be changed to alter or invalidate the teacher evaluation based on value added?*

# Hypothetical example of student replacement



Use the scale for Math, grade 3, in the 2017 M-STEP.



# Motivate student replacement idea

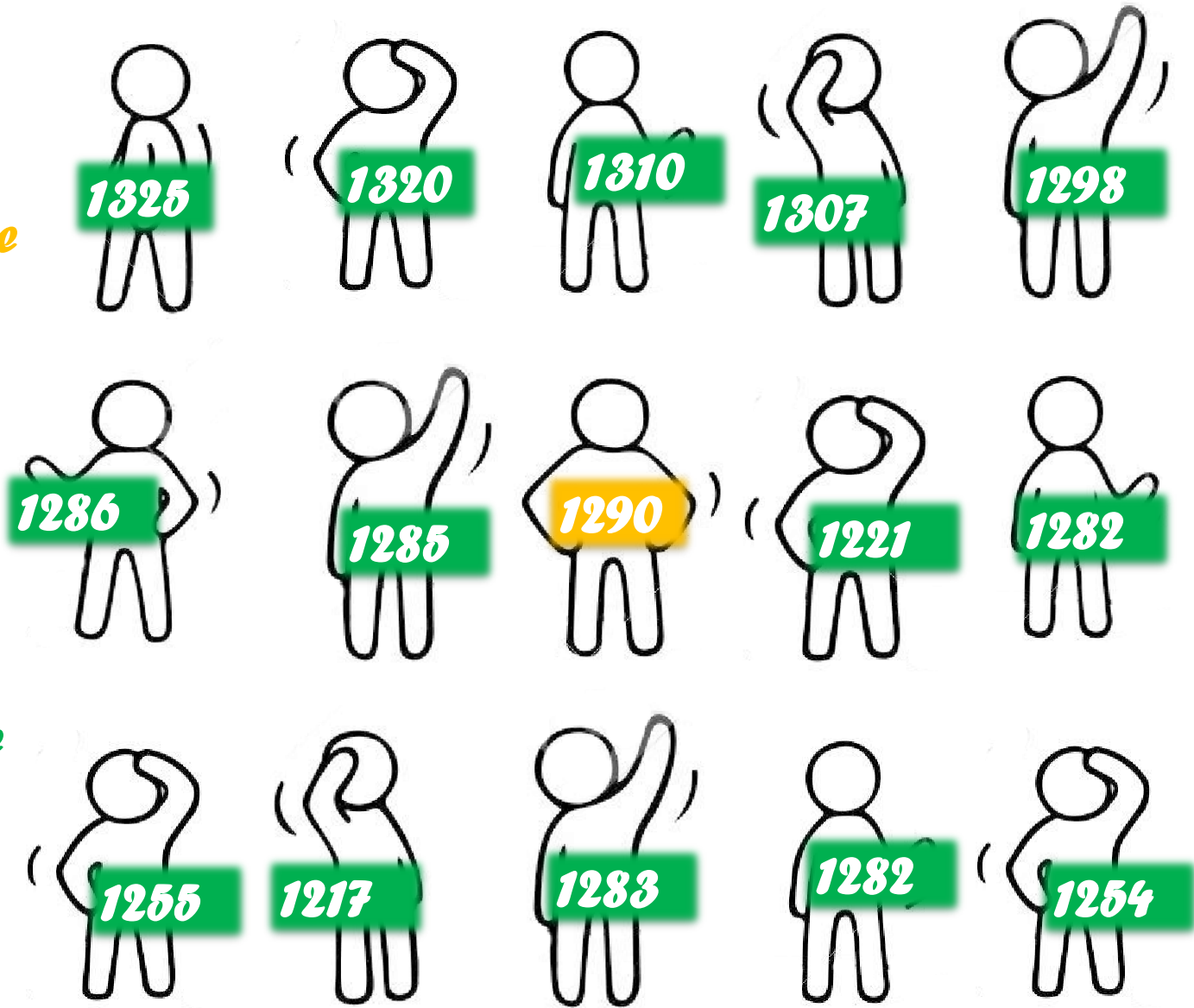
- **Ashley:** I have a grade average effectiveness. I can achieve the threshold if I have more grade average students.
- **Administrator:** No. The below-threshold VAM indicates an inefficient effectiveness.
- The debate is about the uncertainty of VAM.
- *“How many grade average students need to be replaced to alter Ashley’s evaluation?”*

# Hypothetical example of student replacement - Ashley

After  
replacement  
Class average  
achieves 1281

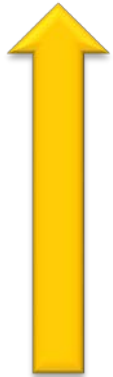


Class average  
= 1280

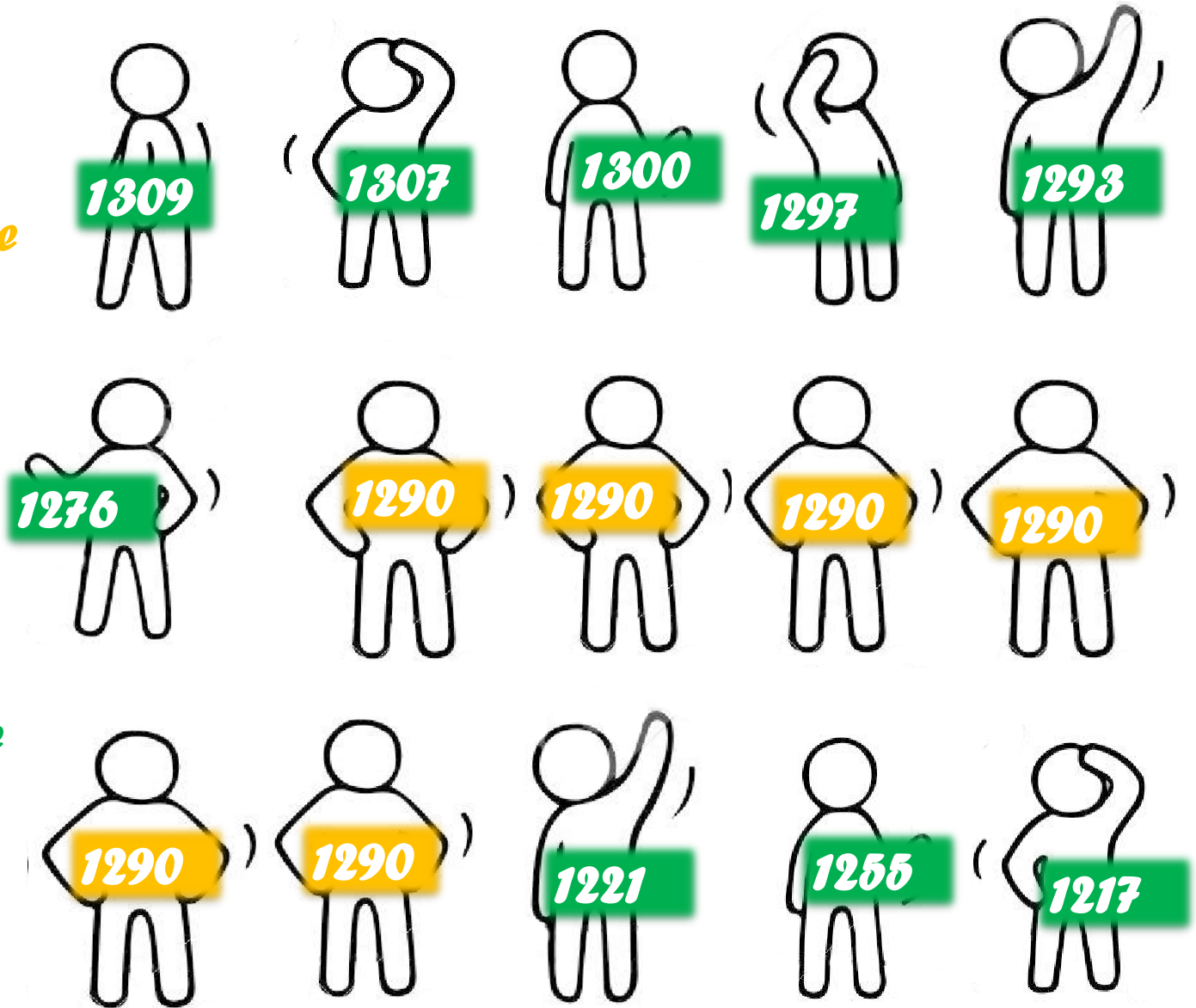


# Hypothetical example of student replacement - Jessica

After  
replacement  
Class average  
improves to  
1281

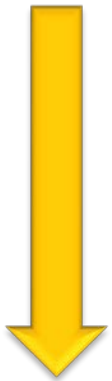


Class average  
= 1275

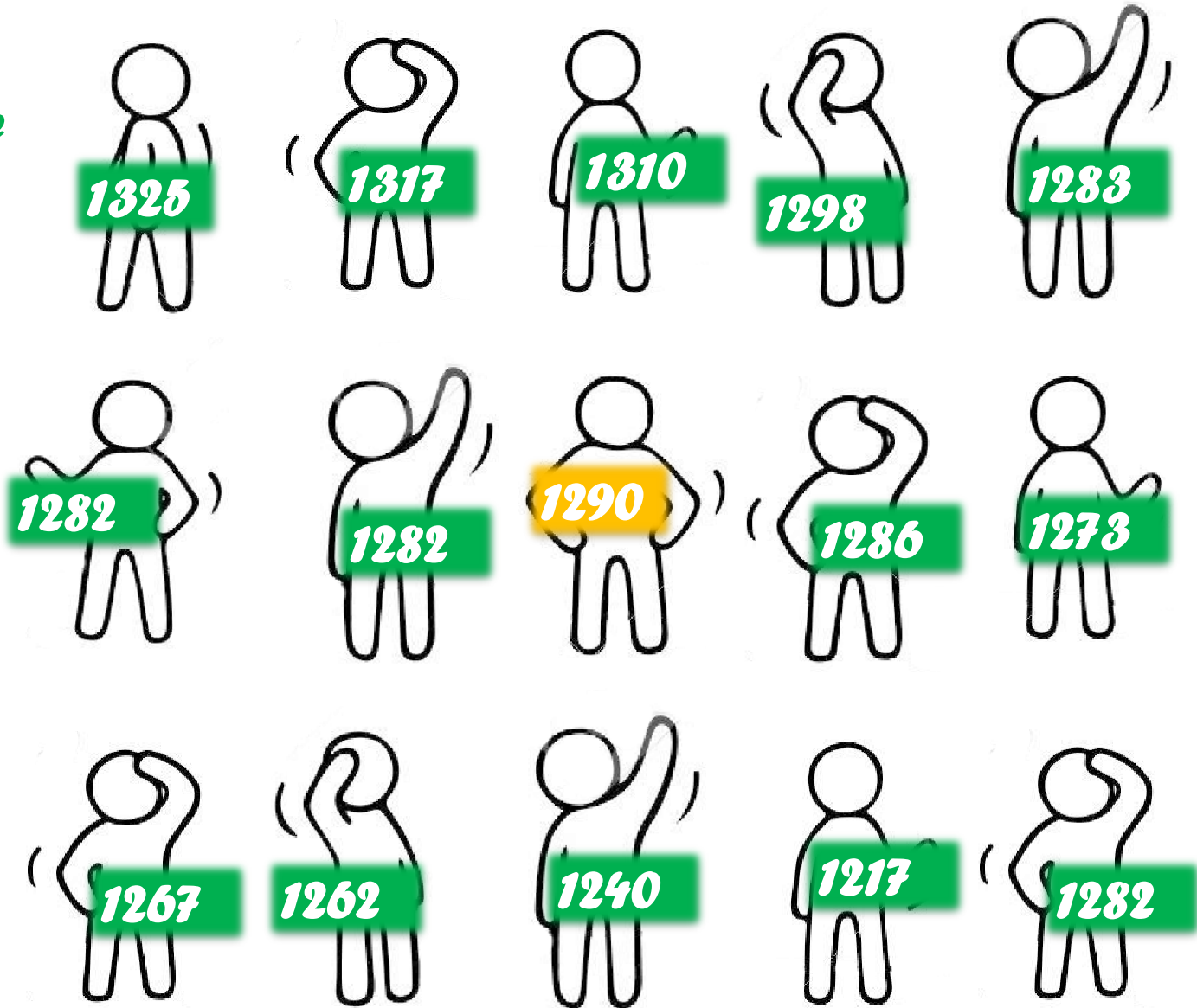


# Hypothetical example of student replacement - Emily

Class average  
= 1282



After  
replacement  
Class average  
drops to 1281



*Ashley: just by replacing **one** of her students, she can achieve the threshold.*

*Jessica: we need to replace **six** of her students to get her to the threshold.*

*Emily: just by replacing **one** of her students, she will drop to the threshold.*

*How can we interpret the number of students need to be replaced?*

- Uncertainty*
- Distance to threshold*

# Why this replacement idea (the mechanism of assigning students to teachers)?

- Easy to understand and interpret
- Directly related to the fundamental assumption of conditional random assignment
  - general framework for those specific sources of bias
- Recognize the agency of teachers, administrators and parents in authentic settings
- The replacement approach can be easily generalized for different contexts (next slide)

# Generalize the student replacement idea

- *“How many grade average students need to be replaced to alter Ashley’s evaluation?”*
  - Why grade average student? (choice of replacement student)
  - How to select students from Ashley’s class to be replaced? (choice of students being replaced)
- Different contexts:
  - Concern about spillover effect?
  - Concern about violation of constant effect assumption?



# Thank you very much!

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If interested, please refer to the draft paper for more details.

Any suggestions and comments are very welcome!